Year 1 - 6

# Calculation Policy Addition and Subtraction

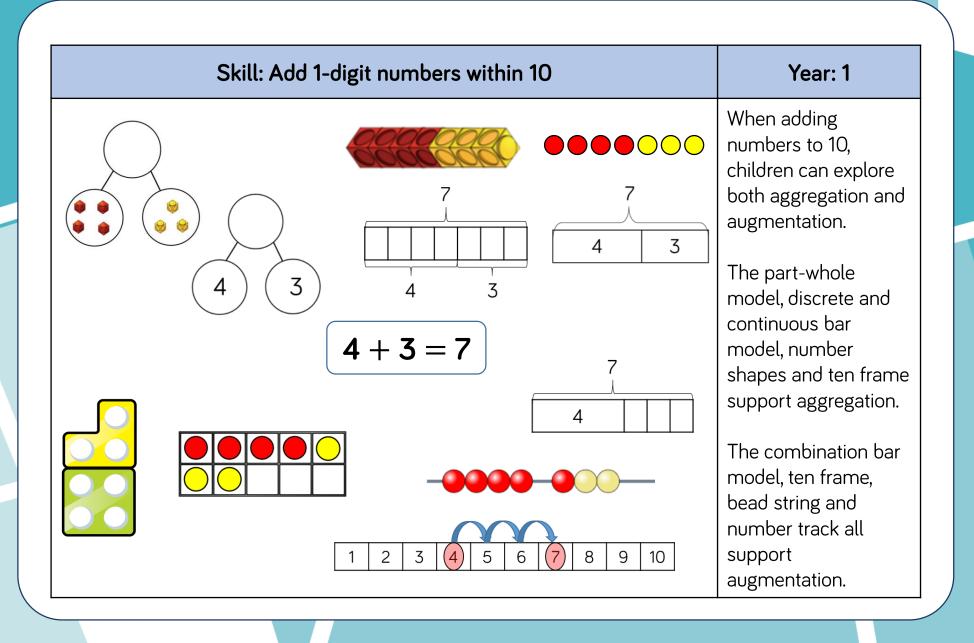
#MathsEveryoneCan

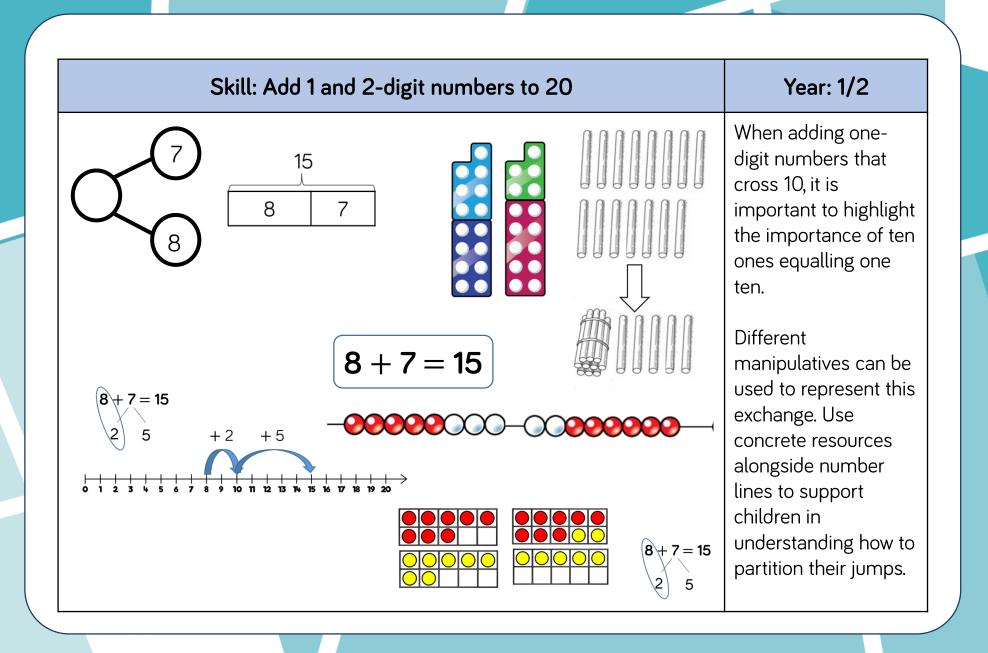


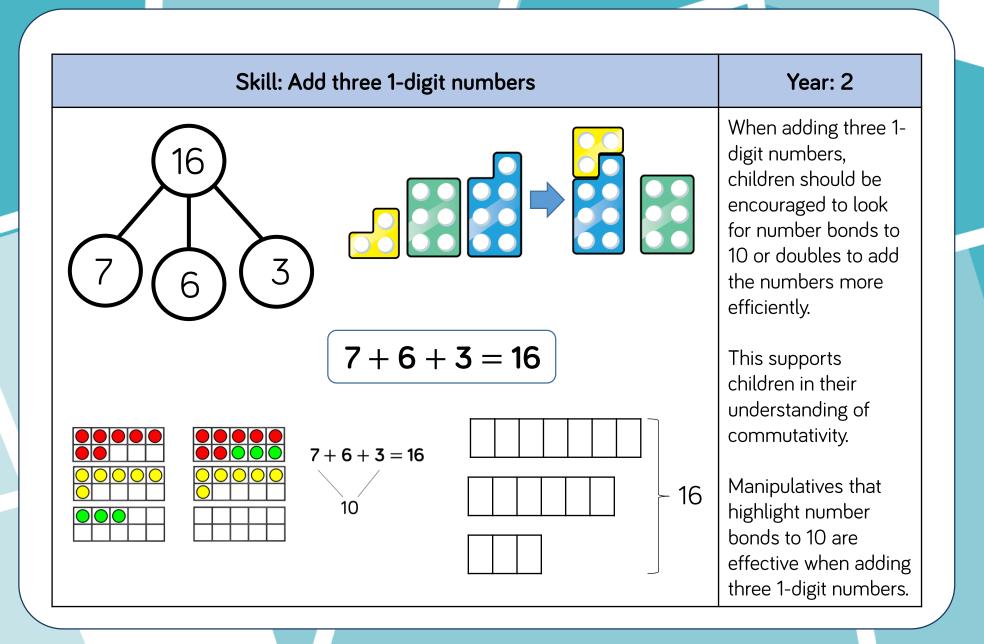
## Addition

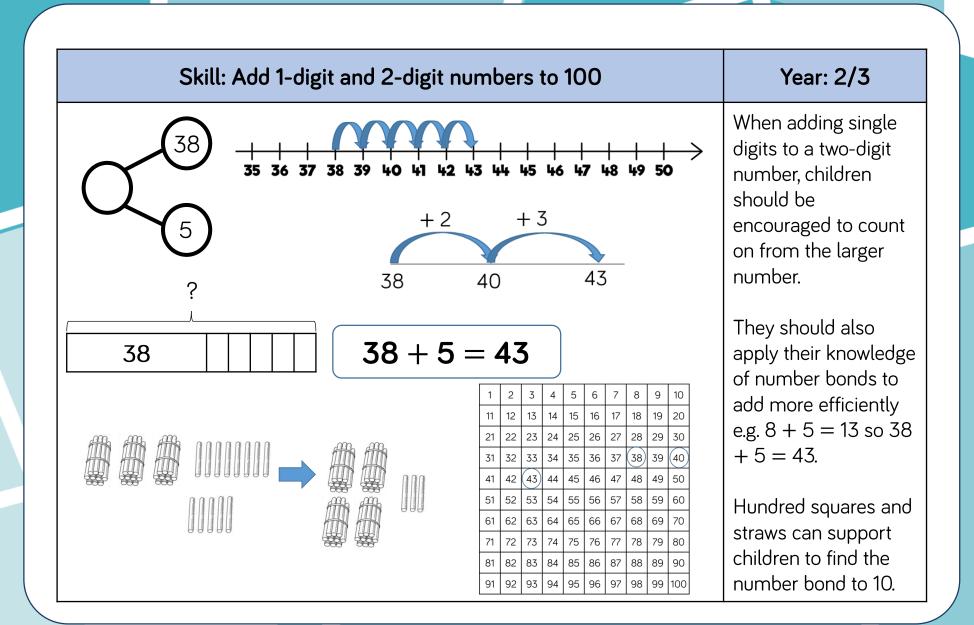
Skill	Year	Representations and models		
Add two 1-digit numbers to 10	1	Part-whole model Bar model Number shapes	Ten frames (within 10) Bead strings (10) Number tracks	
Add 1 and 2-digit numbers to 20	1	Part-whole model Bar model Number shapes Ten frames (within 20)	Bead strings (20) Number tracks Number lines (labelled) Straws	
Add three 1-digit numbers	2	Part-whole model Bar model	Ten frames (within 20) Number shapes	
Add 1 and 2-digit numbers to 100	2	Part-whole model Bar model Number lines (labelled)	Number lines (blank) Straws Hundred square	

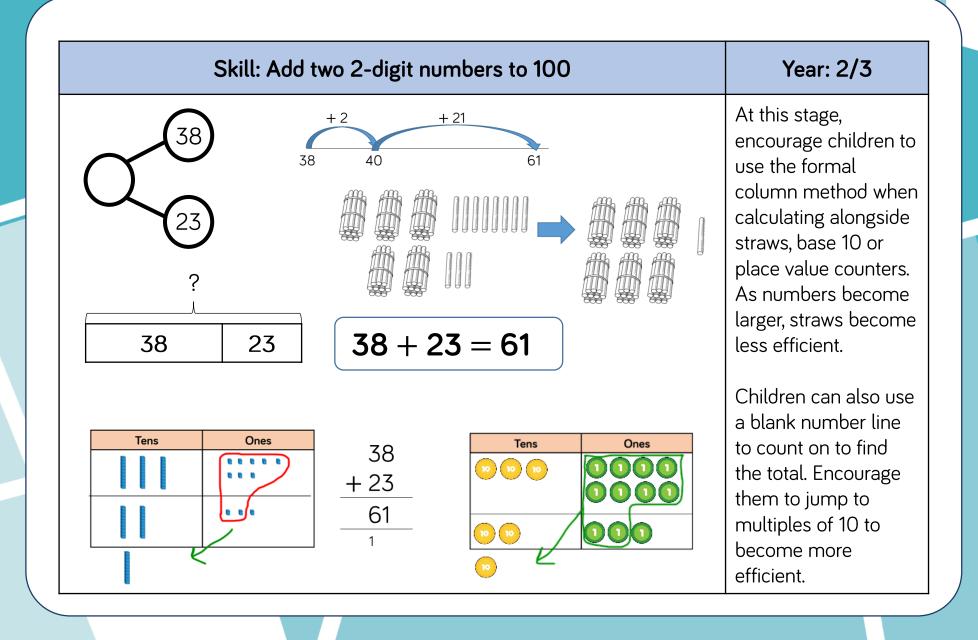
Skill	Year	Representations and models		
Add two 2-digit numbers	2	Part-whole model Bar model Number lines (blank) Straws	Base 10 Place value counters Column addition	
Add with up to 3-digits	3	Part-whole model Bar model	Base 10 Place value counters Column addition	
Add with up to 4-digits	4	Part-whole model Bar model	Base 10 Place value counters Column addition	
Add with more than 4 digits	5	Part-whole model Bar model	Place value counters Column addition	
Add with up to 3 decimal places	5	Part-whole model Bar model	Place value counters Column addition	

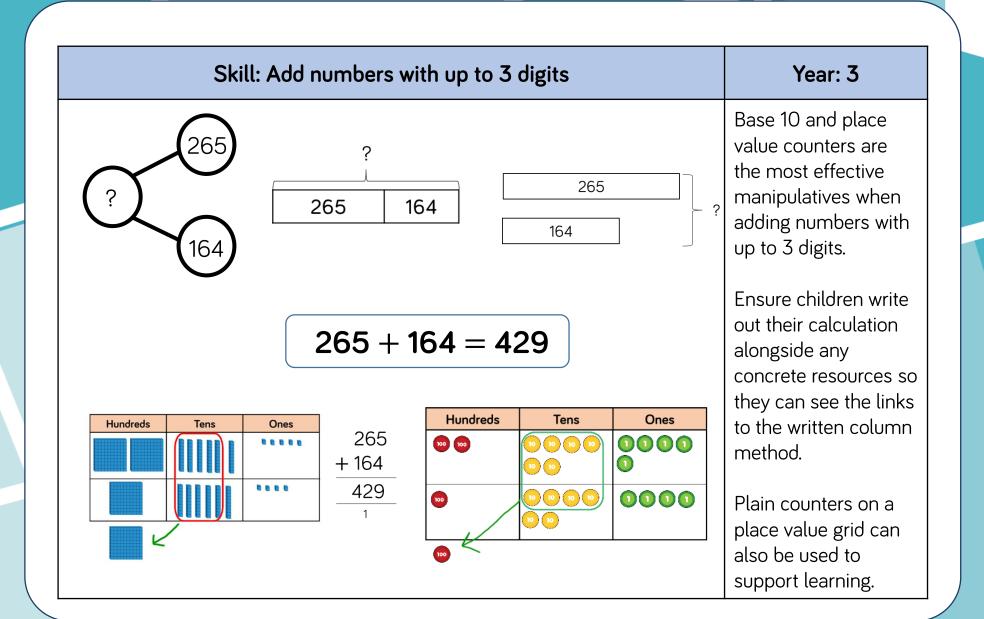


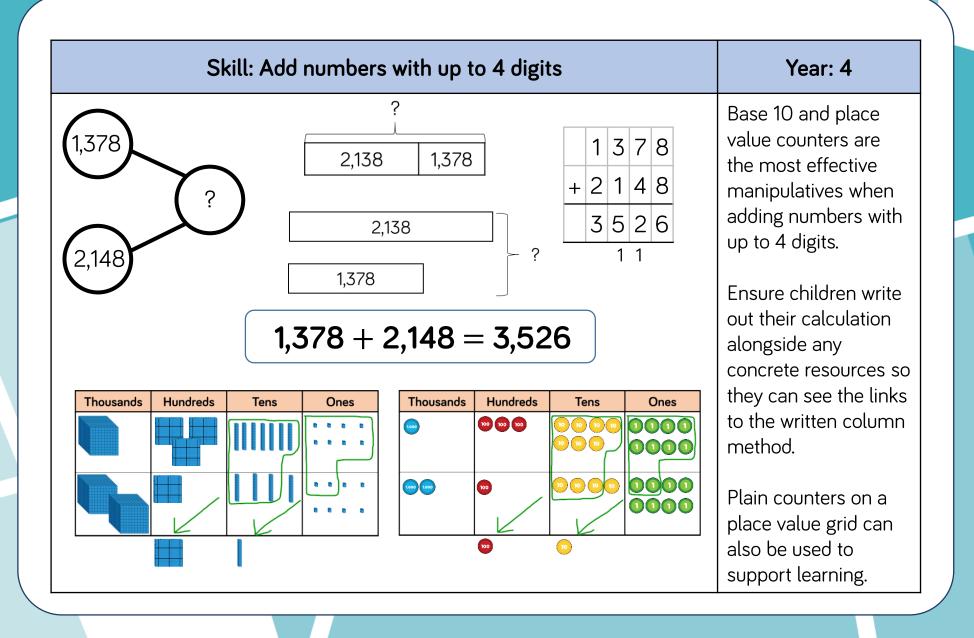


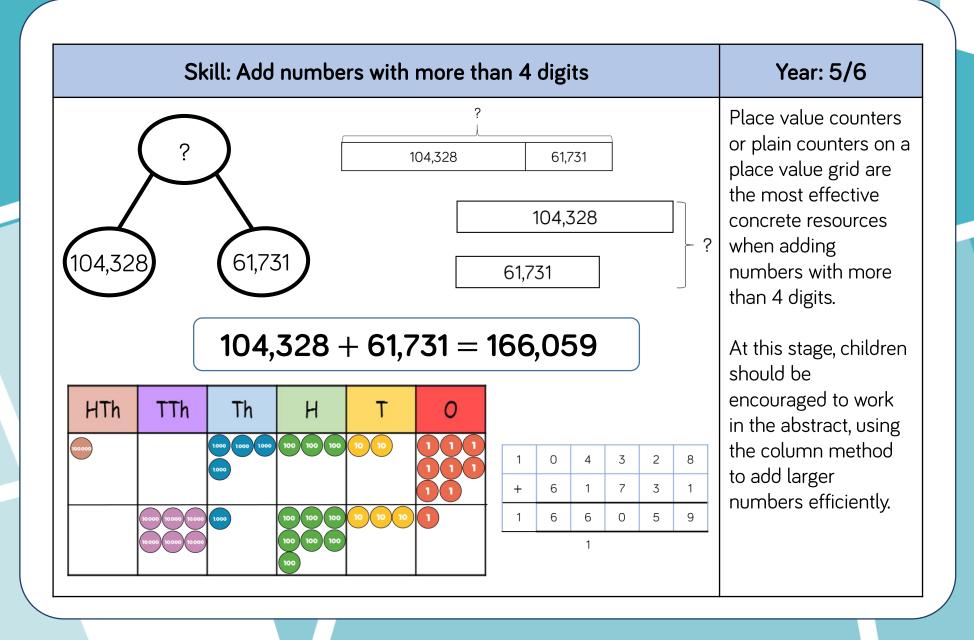


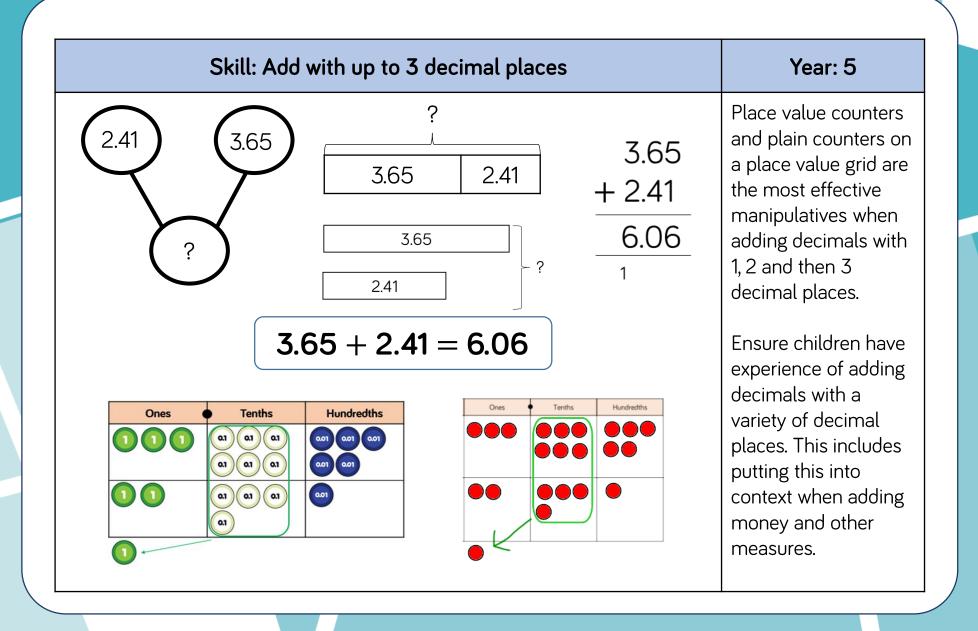








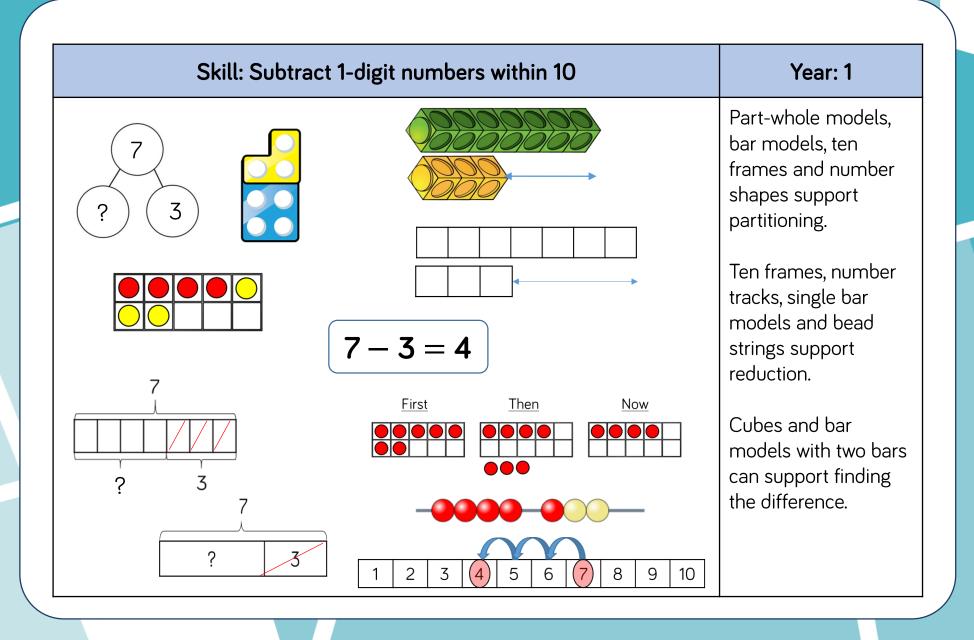


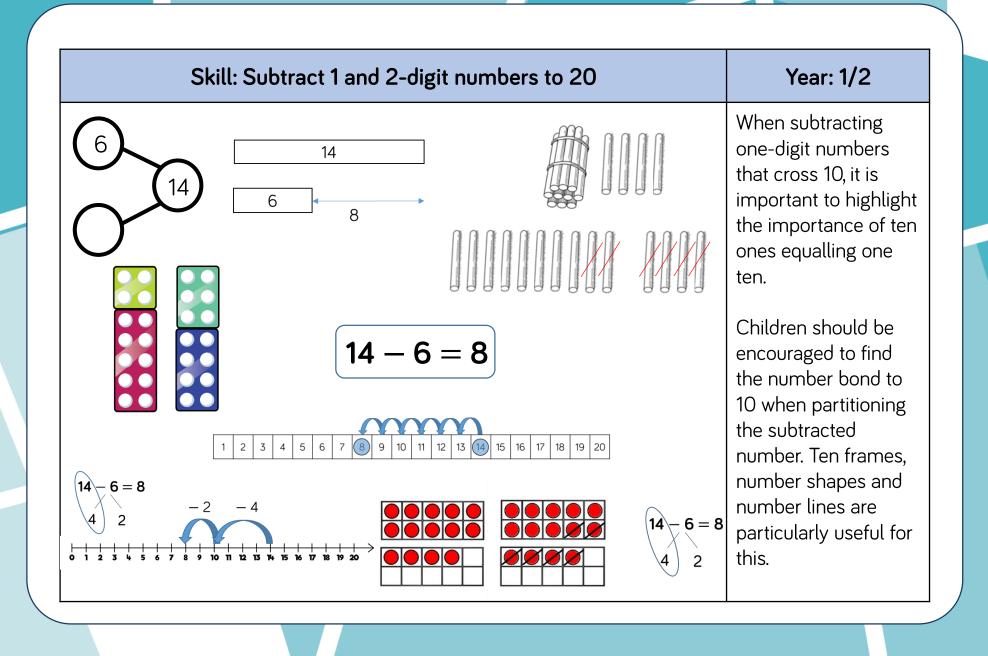


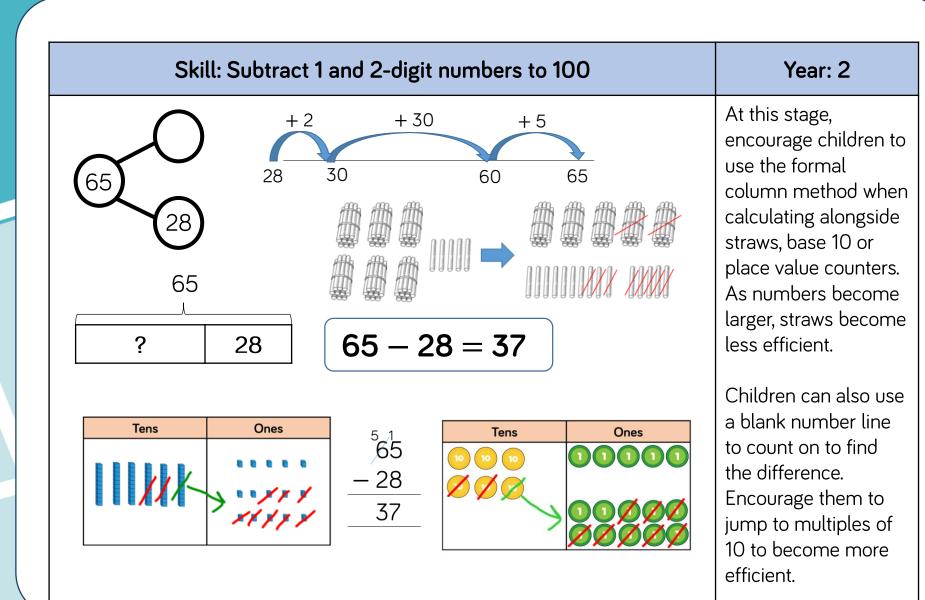
### Subtraction

Skill	Year	Representations and models		
Subtract two 1-digit numbers to 10	1	Part-whole model Bar model Number shapes	Ten frames (within 10) Bead strings (10) Number tracks	
Subtract 1 and 2-digit numbers to 20	1	Part-whole model Bar model Number shapes Ten frames (within 20)	Bead string (20) Number tracks Number lines (labelled) Straws	
Subtract 1 and 2-digit numbers to 100	2	Part-whole model Bar model Number lines (labelled)	Number lines (blank) Straws Hundred square	
Subtract two 2-digit numbers	2	Part-whole model Bar model Number lines (blank) Straws	Base 10 Place value counters Column addition	

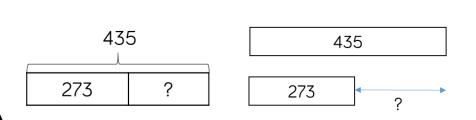
Skill	Year	Representations and models		
Subtract with up to 3- digits	3	Part-whole model Bar model	Base 10 Place value counters Column addition	
Subtract with up to 4- digits	4	Part-whole model Bar model	Base 10 Place value counters Column addition	
Subtract with more than 4 digits	5	Part-whole model Bar model	Place value counters Column addition	
Subtract with up to 3 decimal places	5	Part-whole model Bar model	Place value counters Column addition	











$$435 - 273 = 262$$

Hundreds	Tens	Ones	3/135
		111	– 273
	→    { <del> </del>		262
	11/11/		

435

Hundreds	Tens	Ones
	000 000 ØØØØØ	00Ø; Ø

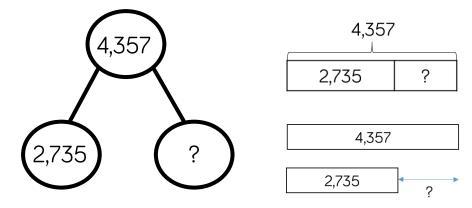
Year: 3

Base 10 and place value counters are the most effective manipulative when subtracting numbers with up to 3 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.





#### Year: 4

Base 10 and place value counters are the most effective manipulatives when subtracting numbers with up to 4 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.



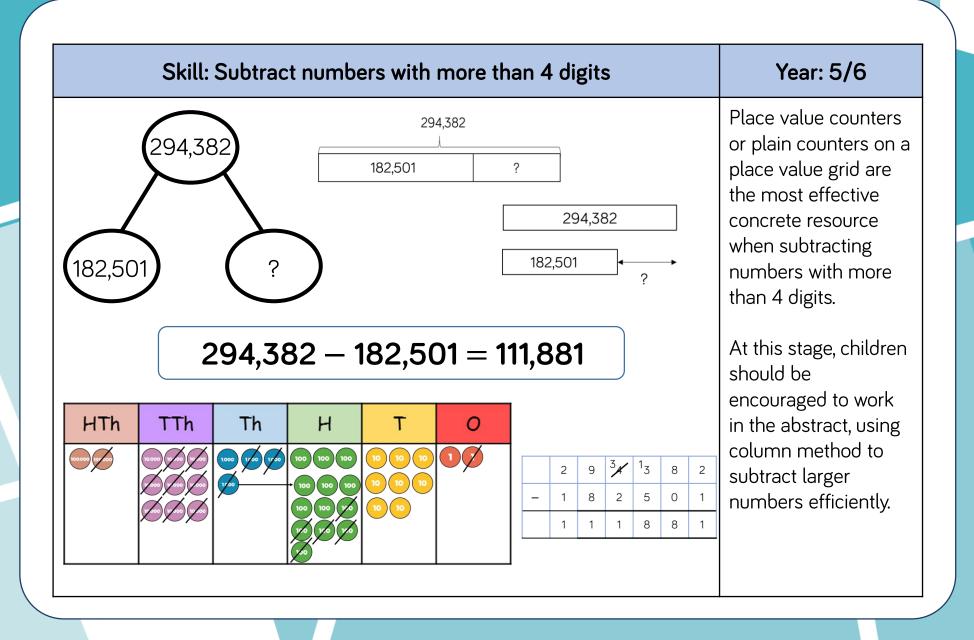
Thousands	Hundreds	Tens	Ones
		11/1/	
		6,000	* * *
	///		
$\rightarrow$			

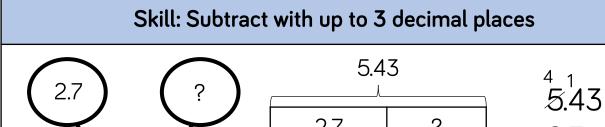
Thousands	Hundreds	Tens	Ones
	100 100 100	0000	0000
1		Ø	$\emptyset$
4			
•	ØØ		

<sup>3</sup>/<sub>4</sub>357

1622

**- 2735** 





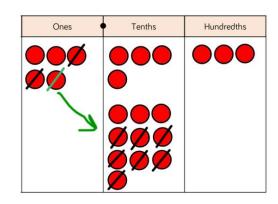
2.7 ? 5.43 -2.7 2.73

5.43 - 2.7 = 2.73

2.7

Ones •	Tenths	Hundredths
	01 01 01 01	0.01 0.01
	0.1 0.1 0.1 0.1	
*	01 01 01 01	
	0.1 0.1	

5.43



Year: 5

Place value counters and plain counters on a place value grid are the most effective manipulative when subtracting decimals with 1, 2 and then 3 decimal places.

Ensure children have experience of subtracting decimals with a variety of decimal places. This includes putting this into context when subtracting money and other measures.

#### Glossary

Addend - A number to be added to another.

**Aggregation -** combining two or more quantities or measures to find a total.

**Augmentation -** increasing a quantity or measure by another quantity.

**Commutative -** numbers can be added in any order.

**Complement –** in addition, a number and its complement make a total e.g. 300 is the complement to 700 to make 1,000

**Difference** – the numerical difference between two numbers is found by comparing the quantity in each group.

**Exchange –** Change a number or expression for another of an equal value.

**Minuend** – A quantity or number from which another is subtracted.

**Partitioning –** Splitting a number into its component parts.

**Reduction -** Subtraction as take away.

**Subitise** – Instantly recognise the number of objects in a small group without needing to count.

**Subtrahend -** A number to be subtracted from another.

**Sum -** The result of an addition.

**Total –** The aggregate or the sum found by addition.

Year 1 - 6

# Calculation Policy Multiplication and Division

#MathsEveryoneCan



# Multiplication

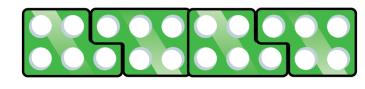
Skill	Year	Representations and models		
Solve one-step problems with multiplication	1/2	Bar model Number shapes Counters	Ten frames Bead strings Number lines	
Multiply 2-digit by 1- digit numbers	3/4	Place value counters Base 10	Short written method Expanded written method	
Multiply 3-digit by 1- digit numbers	4	Place value counters Base 10	Short written method	
Multiply 4-digit by 1- digit numbers	5	Place value counters	Short written method	

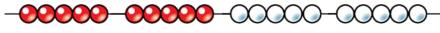
Skill	Year	Representations and models	
Multiply 2-digit by 2- digit numbers	5	Place value counters Base 10	Short written method Grid method
Multiply 2-digit by 3- digit numbers	5	Place value counters	Short written method Grid method
Multiply 2-digit by 4- digit numbers	5/6	Formal written method	

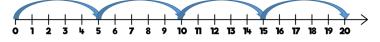
#### Skill: Solve 1-step problems using multiplication



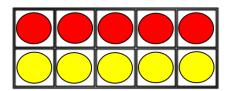


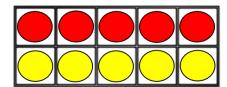






One bag holds 5 apples. How many apples do 4 bags hold?

















$$5 + 5 + 5 + 5 = 20$$

$$4 \times 5 = 20$$

$$5 \times 4 = 20$$

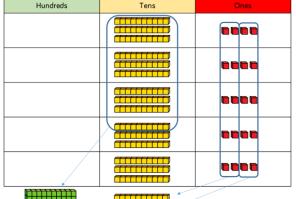
Year: 1/2

Children represent multiplication as repeated addition in many different ways.

In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record multiplication formally.

In Year 2, children are introduced to the multiplication symbol.

#### Skill: Multiply 2-digit numbers by 1-digit numbers



	н	т	0		
		3	4		
×			5		
		2	0	(5	× 4)
+	1	5	0	(5 >	(30)
	1	7	0		



$$34 \times 5 = 170$$

	Н	Т	0	
		3	4	
×			5	
	1	7	0	
	1	2		

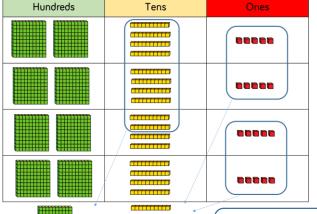
Hundreds	Tens	Ones
	000	0000
	000	0000
	000	0000
	000	0000
	000	0000
0	20	

Year: 3/4

Teachers may decide to first look at the expanded column method before moving on to the short multiplication method.

The place value counters should be used to support the understanding of the method rather than supporting the multiplication, as children should use times table knowledge.

#### Skill: Multiply 3-digit numbers by 1-digit numbers



	Н	Т	О
	2	4	5
×			4
	9	8	0
	1	2	

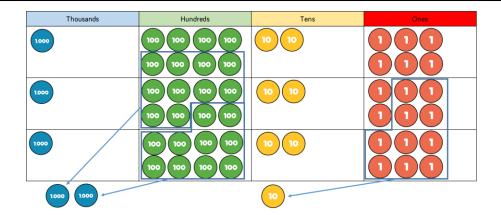
 $245 \times 4 = 980$ 

Hundreds	Tens	Ones
100 100	10 10 10	
100 100	0000	00000
100 100	10 10 10	00000
100 100	00000	00000
100	10 10	

#### Year: 3/4

When moving to 3digit by 1-digit multiplication, encourage children to move towards the short, formal written method. Base 10 and place value counters continue to support the understanding of the written method. Limit the number of exchanges needed in the questions and move children away from resources when multiplying larger numbers.

#### Skill: Multiply 4-digit numbers by 1-digit numbers



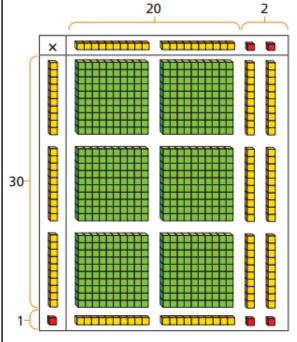
 $1,826 \times 3 = 5,478$ 

	Th	Н	Т	О
	1	8	2	6
×				3
	5	4	7	8
	2		1	

Year: 5

When multiplying 4digit numbers, place value counters are the best manipulative to use to support children in their understanding of the formal written method. If children are multiplying larger numbers and struggling with their times tables, encourage the use of multiplication grids so children can focus on the use of the written method.

#### Skill: Multiply 2-digit numbers by 2-digit numbers



	10 10	1
10	100 100	10 10
10	100 100	10 10
10	100 100	10 10
1	10 10	1 1

×	20	2
30	600	60
1	20	2

$\dashv$		_
		2
	6	6
	6	8

×

Н

Т

2

3

O

#### Year: 5

When multiplying a multi-digit number by 2-digits, use the area model to help children understand the size of the numbers they are using. This links to finding the area of a rectangle by finding the space covered by the Base 10. The grid method matches the area model as an initial written method before moving on to the formal written multiplication method.

 $22 \times 31 = 682$ 

#### Skill: Multiply 3-digit numbers by 2-digit numbers

	100 100	10 10 10	
10 10 10	1000 1000		10 10 10 10 10 10 10 10 10 10 10 10
	100 100	10 10 10	

Th	Н	Т	0
	2	3	4
×		3	2
	4	6	8
1 7	1 <sup>0</sup>	2	0
7	4	8	8

×	200	30	4
30	6,000	900	120
2	400	60	8

Year: 5

Children can continue to use the area model when multiplying 3-digits by 2-digits. Place value counters become more efficient to use but Base 10 can be used to highlight the size of numbers.

Encourage children to move towards the formal written method, seeing the links with the grid method.

 $234 \times 32 = 7,488$ 

TTh	Th	Н	Т	0
	2	7	3	9
×			2	8
2	<b>1</b>	9	1 7	2
5 1	4	7	8	0
7	6	6	9	2

Skill: Multiply 4-digit numbers by 2-digit numbers

When multiplying 4-digits by 2-digits, children should be confident in the written method.

Year: 5/6

If they are still struggling with times tables, provide multiplication grids to support when they are focusing on the use of the method.

Consider where exchanged digits are placed and make sure this is consistent.

 $2,739 \times 28 = 76,692$ 

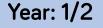
### **Division**

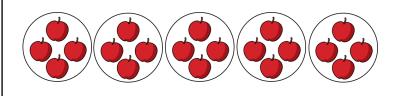
Skill	Year	Representations and models		
Solve one-step problems with division (sharing)	1/2	Bar model Real life objects	Arrays Counters	
Solve one-step problems with division (grouping)	1/2	Real life objects Number shapes Bead strings Ten frames	Number lines Arrays Counters	
Divide 2-digits by 1- digit (no exchange sharing)	3	Straws Base 10 Bar model	Place value counters Part-whole model	
Divide 2-digits by 1- digit (sharing with exchange)	3	Straws Base 10 Bar model	Place value counters Part-whole model	

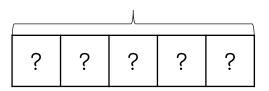
Skill	Year	Representations and models		
Divide 2-digits by 1- digit (sharing with remainders)	3/4	Straws Base 10 Bar model	Place value counters Part-whole model	
Divide 2-digits by 1- digit (grouping)	4/5	Place value counters Place value grid Counters Written short division		
Divide 3-digits by 1- digit (sharing with exchange)	4	Base 10 Bar model	Place value counters Part-whole model	
Divide 3-digits by 1- digit (grouping)	4/5	Place value counters Counters	Place value grid Written short division	

Skill	Year	Representations and models		
Divide 4-digits by 1- digit (grouping)	5	Place value counters Counters	Place value grid Written short division	
Divide multi-digits by 2-digits (short division)	6	Written short division	List of multiples	
Divide multi-digits by 2-digits (long division)	6	Written long division	List of multiples	

## Skill: Solve 1-step problems using multiplication (sharing)





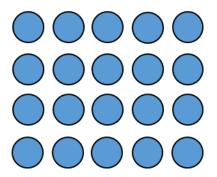


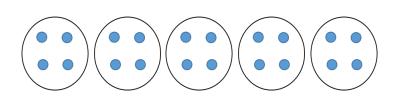
20

There are 20 apples altogether.

They are shared equally between 5 bags.

How many apples are in each bag?



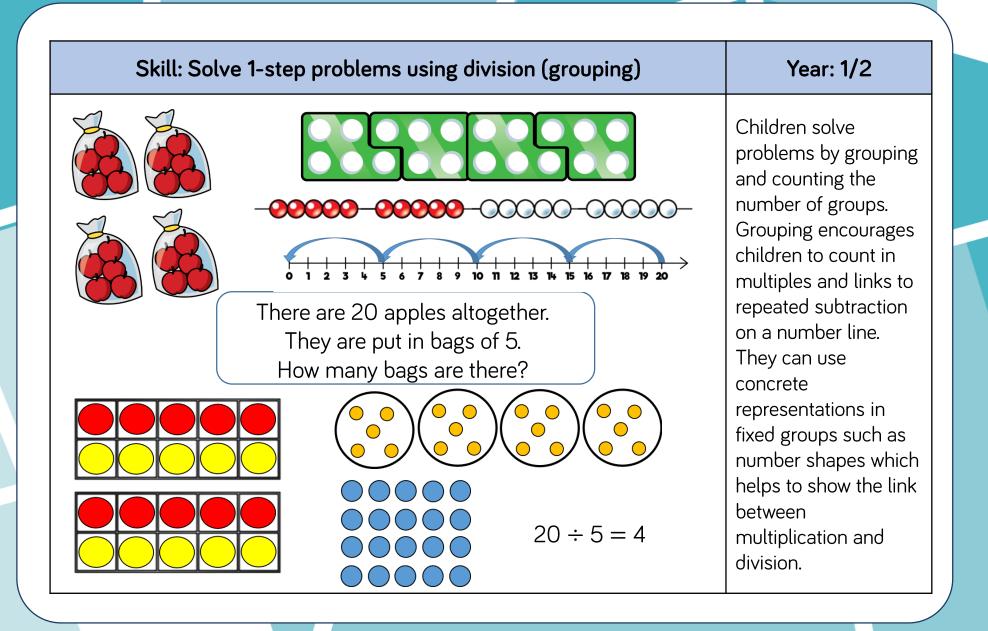


$$20 \div 5 = 4$$

Children solve problems by sharing amounts into equal groups.

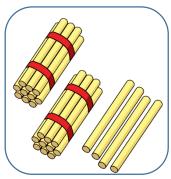
In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record division formally.

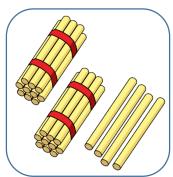
In Year 2, children are introduced to the division symbol.

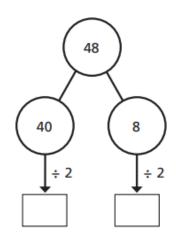


## Skill: Divide 2-digits by 1-digit (sharing with no exchange)

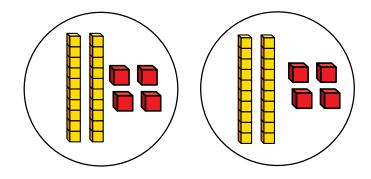
Tens	Ones	
000	000	
000	000	







$$48 \div 2 = 24$$



### **Year: 1/2**

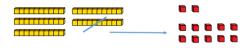
When dividing larger numbers, children can use manipulatives that allow them to partition into tens and ones.

Straws, Base 10 and place value counters can all be used to share numbers into equal groups.

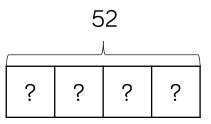
Part-whole models can provide children with a clear written method that matches the concrete representation.

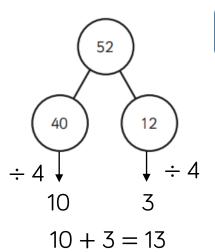


 $52 \div 4 = 13$ 



Tens	Ones	



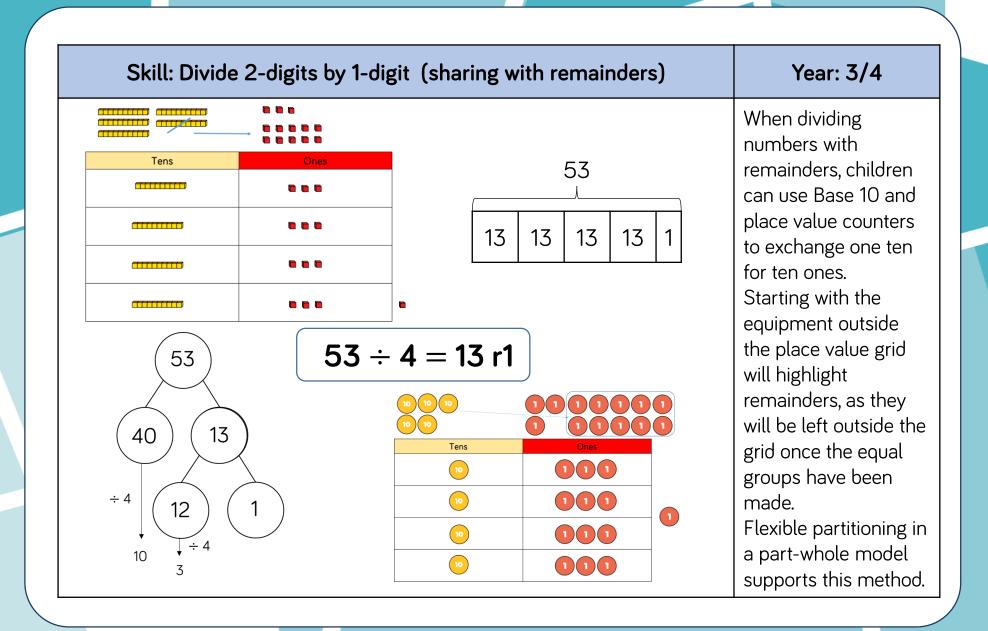


Tens	Ones
10	111
10	111
10	111
10	111

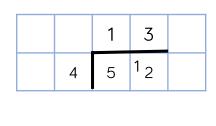
Year: 3/4

When dividing numbers involving an exchange, children can use Base 10 and place value counters to exchange one ten for ten ones.
Children should start with the equipment outside the place value grid before sharing the tens and ones equally between the rows.

Flexible partitioning in a part-whole model supports this method.

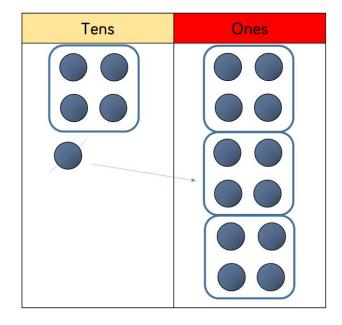


## Skill: Divide 2-digits by 1-digit (grouping)



Tens	Ones
10 10	
10 10	1
10	1

$$52 \div 4 = 13$$



When using the short division method, children use grouping. Starting with the largest place value, they group by the

divisor.

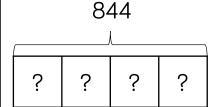
Year: 4/5

Language is important here.
Children should consider 'How many groups of 4 tens can we make?' and 'How many groups of 4 ones can we make?'

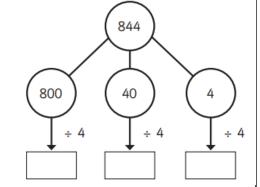
Remainders can also be seen as they are left ungrouped.

## Skill: Divide 3-digits by 1-digit (sharing)

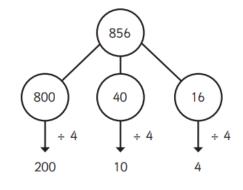
$$844 \div 4 = 211$$

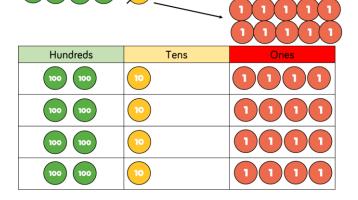


Н	Т	0
100 100	10	1
100 100	10	1
100 100	10	1
100 100	10	1



$$844 \div 4 = 211$$



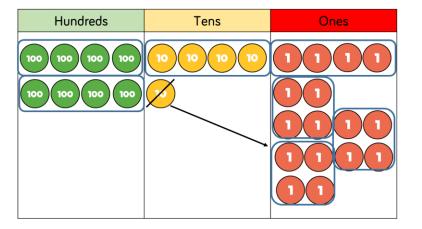


#### Year: 4

Children can continue to use place value counters to share 3digit numbers into equal groups. Children should start with the equipment outside the place value grid before sharing the hundreds, tens and ones equally between the rows. This method can also help to highlight remainders. Flexible partitioning in a part-whole model

supports this method.

## Skill: Divide 3-digits by 1-digit (grouping)





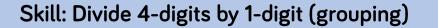
Hundreds Tens Ones

856 ÷ 4 = 214

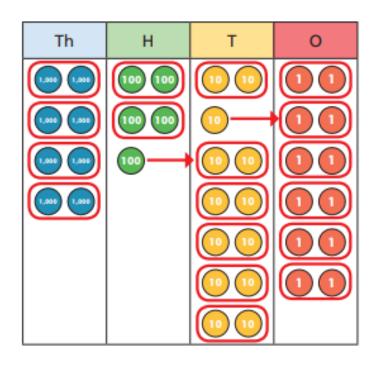
Year: 5

Children can continue to use grouping to support their understanding of short division when dividing a 3-digit number by a 1-digit number.

Place value counters or plain counters can be used on a place value grid to support this understanding. Children can also draw their own counters and group them through a more pictorial method.







	4	2	6	6
2	8	5	13	12

Place value counters or plain counters can be used on a place value grid to support children to divide 4-digits by 1-digit.
Children can also draw their own counters and group them through a more pictorial method.

Children should be encouraged to move away from the concrete and pictorial when dividing numbers with multiple exchanges.

$$8,532 \div 2 = 4,266$$

#### Skill: Divide multi digits by 2-digits (short division) Year: 6 When children begin to divide up to 4digits by 2-digits, 3 06 written methods $432 \div 12 = 36$ become the most 4 3 12 4 accurate as concrete and pictorial representations become less effective. Children can write out multiples to support their calculations with larger remainders. 0 4 8 9 Children will also $7,335 \div 15 = 489$ 7 3 13 13<sub>5</sub> solve problems with 15 remainders where the quotient can be 15 30 75 45 60 90 105 120 135 150 rounded as appropriate.

		0	3	6
1	2	4	3	2
	_	3	6	0
			7	2
	_		7	2
				0

$12 \times 3 = 36$	
$12 \times 4 = 48$	470 . 10 70
$12 \times 5 = 60$	$432 \div 12 = 36$

$$(\times 6)$$
 12 × 6 = 72  
12 × 7 = 84

(x30)

 $12 \times 1 = 12$  $12 \times 2 = 24$ 

$$12 \times 8 = 96$$
  
 $12 \times 7 = 108$ 

$$12 \times 10 = 120$$

$$7,335 \div 15 = 489$$

	0	4	8	9	
15	7	3	3	5	
_	6	0	0	0	(×4
	1	3	3	5	
_	1	2	0	0	(×8
		1	3	5	
_		1	3	5	(×9
				0	

$$2 \times 15 = 30$$

$$3 \times 15 = 45$$

$$4 \times 15 = 60$$

$$5 \times 15 = 75$$

$$10 \times 15 = 150$$

Children can also divide by 2-digit numbers using long division.

Year: 6

Children can write out multiples to support their calculations with larger remainders.

Children will also solve problems with remainders where the quotient can be rounded as appropriate.

## Skill: Divide multi digits by 2-digits (long division)

Year: 6

 $372 \div 15 = 24 \text{ r}12$ 

			2	4	r	1	2
1	5	3	7	2			
	_	3	0	0			
			7	2			
	_		6	0			
			1	2			

$$1 \times 15 = 15$$
  
 $2 \times 15 = 30$   
 $3 \times 15 = 45$   
 $4 \times 15 = 60$   
 $5 \times 15 = 75$   
 $10 \times 15 = 150$ 

When a remainder is left at the end of a calculation, children can either leave it as a remainder or convert it to a fraction.
This will depend on the context of the question.

$$372 \div 15 = 24 \frac{4}{5}$$

Children can also answer questions where the quotient needs to be rounded according to the context.

# Glossary

**Array** – An ordered collection of counters, cubes or other item in rows and columns.

**Commutative –** Numbers can be multiplied in any order.

**Dividend** – In division, the number that is divided.

**Divisor** – In division, the number by which another is divided.

**Exchange –** Change a number or expression for another of an equal value.

**Factor** – A number that multiplies with another to make a product.

**Multiplicand** – In multiplication, a number to be multiplied by another.

**Partitioning –** Splitting a number into its component parts.

**Product** – The result of multiplying one number by another.

**Quotient -** The result of a division

**Remainder** – The amount left over after a division when the divisor is not a factor of the dividend.

**Scaling –** Enlarging or reducing a number by a given amount, called the scale factor